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Implications and Applications of Electroweak Quantum Gravity

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Authors' contributions

This work was carried out in collaboration between both authors. Author UVSS designed the study, performed the statistical analysis, wrote the protocol, wrote the first draft of the manuscript and managed the literature searches. Author SL managed the analyses of the whole study with special focus. Both authors read and approved the final manuscript.

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Review Article

ABSTRACT

We strongly believe that, the success of any unified model depends on its ability to involve gravity in microscopic models. To understand the mystery of final unification, in our earlier publications, we proposed two bold concepts:1) There exist three atomic gravitational constants associated with electroweak, strong and electromagnetic interactions. 2) There exists a strong elementary charge (e_s) in such a way that its squared ratio with normal elementary charge is close to reciprocal of the strong coupling constant. In this review article we propose that, $(\hbar c)$ can be considered as a compound physical constant associated with electroweak gravity. With these new ideas, an attempt is made to understand and fit nuclear stability, binding energy and quark masses. We wish to

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emphasize that, nuclear binding energy can be fitted with four simple terms having one unique energy coefficient, $(e_s^2/4\pi\varepsilon_0R_0) \cong 10.09 \text{ MeV}$. With reference to proton-electron mass ratio, Newtonian gravitational constant can be estimated in a verifiable approach. Recently observed 3.5 keV photon seems to be an outcome of annihilation of a new charged small or tiny lepton of rest energy 1.75 keV. By questioning and understanding the integral nature of electron's angular momentum, existence of the three atomic gravitational constants can be understood. By studying the stellar magnetic dipole moments with reference to weak and strong interactions, there is a possibility of confirming the existence of atomic gravitational constants.

Keywords: Four gravitational constants; compound reduced Planck's constant; nuclear elementary charge; strong coupling constant; electroweak fermion.

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NOMENCLATURES

- 1) Newtonian gravitational constant = G_N
- 2) Electromagnetic gravitational constant= G_{e}
- 3) Nuclear gravitational constant = G_{c}
- 4) Weak gravitational constant = G_w
- 5) Fermi's weak coupling constant = G_{F}
- 6) Reduced Planck's constant = \hbar
- 7) Speed of light = c
- 8) Mass of proton = m_p
- 9) Mass of neutron = m_n
- 10) Mass of electron = m_{e}
- 11) Mass of new electroweak fermion = M_{\odot}
- 12) Normal elementary charge = e
- 13) Strong nuclear elementary charge = e_{c}
- 14) Strong coupling constant = α_s
- 15) Specific charge ratio of proton = (e_x/m_p)
- 16) Specific charge ratio of electron = (e/m_e)
- 17) Ratio of specific charge ratio of proton and electron $=_{s}$
- 18) Proton number = Z
- 19) Mass number = $_A$
- 20) Neutron number = N
- 21) Stable mass number = A_s
- 22) Stable neutron number = N_{c}
- 23) Lower stable mass number = $(A_s)_{lower}$
- 24) Mean stable mass number = $(A_{s})_{max}$
- 25) Upper stable mass number = $(A_s)_{unare}$
- 26) Stability coefficient = k = 4s

- 27) Free nucleon number coefficient = f
- 28) Nuclear binding energy = $B_{\perp} = BE$
- 29) Volume energy coefficient = a_{i}
- 30) Surface energy coefficient = a
- 31) Coulombic energy coefficient = a_c
- 32) Asymmetric energy coefficient = a_{i}
- 33) Pairing energy coefficient = a_{i}
- 34) Nuclear binding energy at $A_{r} = B_{A}$
- 35) Up quark mass = m_{μ}
- 36) Down quark mass = m_{d}
- 37) Strange quark mass = m_{i}
- 38) Charm quark mass = m_{1}
- 39) Bottom quark mass = m_{μ}
- 40) Top quark mass = m_{i}
- 41) Force ratio associated with proton and electron = $X \cong e^2/4\pi\varepsilon_0 G_s m_s m_e$
- 42) Interaction range = r_x
- 43) Characteristic ratio associated with charged leptons = $\sqrt{4\pi\varepsilon_0 G_e m_e^2/e^2} \simeq \gamma$
- 44) Mass of charged small lepton= $(m_{xl})^{\pm}$
- 45) Magnetic moment of proton = μ_n
- 46) Magnetic moment of electron = μ_e
- 47) Mass of stellar object = M_{χ}
- 48) Magnetic moment of stellar objects = μ_x

1. INTRODUCTION TO LARGE GRAVITA-TIONAL COUPLING CONSTANTS

According to Quantum Chromodynamics (QCD) [1], strong interaction exhibits two important characteristics, Color or guark confinement and Asymptotic freedom. Color confinement deals with production of hadrons from hadrons without an isolated color charge. Asymptotic freedom deals with reduction of strength of interaction with increasing energy scales at decreasing length scale. Visualizing hadrons as particle level black holes having large nuclear gravitational coupling constant $G_s \approx 10^{39} G_N$. Tennakone, De Sabbata, Gasperini, Abdus Salam, Sivaram and K.P. Sinha [2-5] tried to explain guark confinement with spin-2 massive particles. Based on this 'strong nuclear gravity' and by following Hawking's black hole temperature formula [6], quark-gluon plasma temperature can be understood with a remarkable relation of the form $T_{qg} \approx \hbar c^3 / 8\pi k_B G_s m_n \approx 10^{12}$ °K. Keeping this [3], 'strong nuclear gravity' approach in view, to understand weak interactions, in 2013, Roberto Onofrio [7] introduced a large electroweak gravitational coupling constant. In our 2011 and 2012 papers [8,9] and recently published papers [10-18]. we introduced a verv large

In this review article, by considering the three atomic gravitational coupling constants, we review our recently published four REFERENCE relations [10] with reference to $(\hbar c)$ and tried to infer the proposed four term semi empirical mass formula with possible physics. In section 8, we tried to fit quark masses. In section 9, we presented many result oriented supporting relations. In sections (10 to 15), we show various practical applications of (G_{-}, G_{-}, G_{-}) .

electromagnetic gravitational coupling constant

for understanding the basics of final unification.

2. HISTORY AND CURRENT STATUS OF NUCLEAR BINDING ENERGY SCHEME

With respect to nuclear binding energy and Semi Empirical Mass Formula (SEMF), the inverse problem framework [19], allows to infer the underlying model parameters from experimental observation, rather than to predict the observations from the model parameters. Recently, the ground-state properties of nuclei with Z= 8 to 120 from the proton drip line to the neutron drip line have been investigated using the spherical relativistic continuum Hartree-

Bogoliubov (RCHB) theory [20] with the relativistic density functional PC-PK1 (A new parameterization for the nuclear covariant energy density functional with nonlinear point-coupling interaction scheme proposed by fitting to observables of 60 selected spherical nuclei, including the binding energies, charge radii and empirical pairing gaps). In this context, in our recently published paper [10], we emphasized the fact that, physics and mathematics associated with fixing of the energy coefficients of SEMF are neither connected with residual strong nuclear force nor connected with strong coupling constant. N. Ghahramany and team members are constantly working on exploring the secrets of nuclear binding energy and magic numbers in terms of quarks [21,22]. Very interesting point of their study is that - nuclear binding energy can be understood with two or three terms having single energy coefficient of the order of 10 MeV.

3. MOTIVATING CONCEPTS / BASIC IDEAS/ASSUMPTIONS

Even though celestial objects that show gravity are confirmed to be made up of so many atoms, so far scientists could not find any relation between gravity and the atomic interactions. It clearly indicates that, there is something wrong in our notion of understanding or developing the unified physical concepts. To develop new and workable ideas, we emphasize that,

- Whether particle's massive nature is due to electromagnetism or gravity or weak interaction or strong interaction or cosmic dust or something else, is unclear.
- 2) Without understanding the massive nature, it is not reasonable to classify the field created by any elementary particle.
- 3) All the four interactions seem to be associated with \hbar .
- Nobody knows the mystery of (ħ) which seems to be a basic measure of angular momentum.
- Nobody knows the mystery of existence, stability and behavior of 'proton' or 'electron'.
- 'Mass' is a basic property of space-time curvature and basic ingredient of angular momentum.
- 7) Atoms are mainly characterized by protons and electrons.
- 8) 'Free neutron' is an unstable particle.

Based on these 8 points, we propose the following new and workable concepts.

Hypothesis-1: The four basic interactions can be allowed to have four different gravitational constants.

 $G_e \approx 2.374335 \times 10^{37} \text{ m}^3\text{kg}^{-1}\text{sec}^{-2}$ $G_s \approx 3.329561 \times 10^{28}\text{m}^3\text{kg}^{-1}\text{sec}^{-2}$ $G_w \approx 2.909745 \times 10^{22} \text{ m}^3\text{kg}^{-1}\text{sec}^{-2}$ $G_N \approx 6.679855 \times 10^{-11} \text{ m}^3\text{kg}^{-1}\text{sec}^{-2}$

Hypothesis-2: There exists a strong elementary charge in such a way that its squared ratio with normal elementary charge is close to inverse of the strong coupling constant.

Hypothesis-3: $(\hbar c)$ can be considered as a compound physical constant connecting electroweak interaction.

Hypothesis-4: There exists a characteristic electroweak fermion of rest energy [17], $M_{\omega}c^2 \cong 584.725$ GeV.

Hypothesis-5: Fermi's weak coupling constant (G_{F}) [23,24] can be considered as the basic unified coupling constant.

With these bold ideas, starting from charged lepton rest masses to stellar masses can be understood. In addition to that, Newtonian gravitational constant can be estimated in a *verifiable approach*. We appeal that, by thoroughly analyzing the bold ideas, it may be possible to understand the combined role of the four gravitational constants in understanding the vector and tensor nature of fundamental forces and their interaction ranges.

4. CHARACTERISTIC UNIFIED RELA-TIONS

Based on the above points, we propose the following new and workable relations.

 (*hc*) can be considered as one of the basic interaction coupling constants associated with quantum phenomena. It can be considered as a compound physical constant,

$$\hbar c \cong G_{w}M_{w}^{2} \cong \sqrt{G_{F}\left(\frac{c^{4}}{4G_{w}}\right)}$$
$$\Rightarrow \hbar \cong \frac{G_{w}M_{w}^{2}}{c} \cong \sqrt{\frac{G_{F}c^{2}}{4G_{w}}}$$
(1A)

where $\left(\frac{c^4}{4G_w}\right) \cong 6.9401 \times 10^{10}$ N is the characteristic

force associated with electroweak interaction.

$$m_{e} \cong \left(\frac{G_{w}}{G_{s}}\right) M_{w} \tag{1B}$$

$$m_{p} \cong \left(\frac{G_{s}}{G_{w}}\right) \left(\frac{G_{s}}{G_{e}}\right) M_{w} \cong \left(\frac{G_{s}^{2}}{G_{w}G_{e}}\right) M_{w}$$
(1C)

$$\frac{m_p}{m_e} \cong \frac{G_s^3}{G_w^2 G_e} \tag{1D}$$

(2) There exists a strong elementary charge (e_s) in such a way that,

$$\frac{m_p}{m_e} \approx \left(\frac{G_s m_p^2}{\hbar c}\right) \left(\frac{G_e m_e^2}{\hbar c}\right)$$
$$\approx \left(\frac{e_s^2}{4\pi\varepsilon_0 G_s m_p^2}\right) / \left(\frac{e^2}{4\pi\varepsilon_0 G_e m_e^2}\right)$$
(2)

$$\rightarrow \begin{cases} \frac{e_s^2}{e^2} \approx \left(\frac{G_s m_p^3}{G_e m_e^3}\right) \approx \left(\frac{G_s m_p^2}{\hbar c}\right)^2 \approx \frac{1}{\alpha_s} \\ \frac{e_s}{e} \approx \sqrt{\frac{G_s m_p^3}{G_e m_e^3}} \approx \left(\frac{G_s m_p^2}{\hbar c}\right) \approx \sqrt{\frac{1}{\alpha_s}} \end{cases}$$
(3)

where, $\alpha_s \cong$ Strong coupling constant

Based on these relations,

$$e_s \approx 2.9463591e, \ \alpha_s \approx 0.1151937$$

and $\frac{1}{\alpha_s} \approx 8.681032$

5. UNDERSTANDING PROTON-NEUTRON STABILITY WITH THREE ATOMIC GRAVITATIONAL CONS-TANTS

In our recently published paper [10], we proposed the following semi empirical relations (4) to (10) for fitting nuclear stability and binding energy.

With reference to the ratio of specific charge ratio of proton and specific charge ratio of electron,

$$s \approx \left\{ \left(\frac{e_s}{m_p} \right) \div \left(\frac{e}{m_e} \right) \right\} \approx 0.001605$$

$$\approx \sqrt{\frac{G_s m_p}{G_e m_e}} \approx \frac{G_s m_p m_e}{\hbar c} \approx \frac{\hbar c}{G_e m_e^2} \approx \frac{G_s^2}{G_e G_w} \approx \frac{m_p}{M_w} \right]$$
(4)
where, $M_w \approx \sqrt{\hbar c/G_w} \approx 584.725 \text{ GeV}/c^2$

Nuclear mean beta stability line can be explained with a relation of the form,

$$A_{s} \cong Z + N_{s} \cong 2Z + s(2Z)^{2}$$

$$\cong 2Z + (4s)Z^{2} \cong 2Z + kZ^{2} \cong Z(2 + kZ)$$
(5)
where $k \cong 4s \cong 0.0064185$

With this kind of relation, by guessing the proton number, corresponding stable zone nucleon number can be estimated directly. With even-odd corrections and fine tuning the value of k, better understanding is possible. Considering $k \approx 0.00642$ and by considering a simple quadratic equation, relation (5) can be derived.

Let,
$$x = \frac{Zk}{2}$$

 $C = \frac{Zk}{2} = \frac{Ak}{4} \left(\because \text{ Initially, } Z = \frac{A}{2} \right)$
and $x^2 + x - C \cong 0$
 $\left\{ x^2 \text{ coefficient} = 1 \right\}$
 $x \text{ coefficient} = 1$
 $x \text{ coefficient} = 1$
 $\Rightarrow \frac{Zk}{2} \cong \frac{-1 \pm \sqrt{kA + 1}}{2}$
 $\Rightarrow Z \cong \frac{-1 \pm \sqrt{kA + 1}}{k} \cong \frac{A}{(2.0 + 0.0153A^{2/3})}$
(5A)

By considering a factor like $\left[2\pm\sqrt{k}\right]$, likely possible range of A_s can be explained with,

$$\begin{cases} (A_s)_{lower} \cong Z(1.92 + kZ) \\ (A_s)_{mean} \cong Z(2.0 + kZ) \\ (A_s)_{upper} \cong Z(2.08 + kZ) \end{cases}$$
(6)

6. UNDERSTANDING NUCLEAR BIND-ING ENERGY

For $(Z \approx 3 \text{ to } 118)$, close to beta stability line, nuclear binding energy can be fitted with,

$$B_{A_s} \cong \left\{ \left(1 - 0.00189 \sqrt{ZN_s} \right) A_s - A_s^{1/3} - \left(\frac{Z}{N_s} \right) \right\} 10.09 \text{ MeV} (\textbf{7A})$$

where $0.00189 = \text{New coefficiet} \cong f$

Binding energy per nucleon can be estimated with,

$$\frac{B_{A_s}}{A_s} \approx \frac{1}{A_s} \left\{ \left(1 - 0.00189 \sqrt{ZN_s} \right) A_s - A_s^{1/3} - \left(\frac{Z}{N_s} \right) \right\} 10.09 \text{ MeV} \quad \text{(7B)}$$

See Fig. 1. Dashed red curve plotted with relations (5) and (7B) can be compared with the green curve plotted with the following standard SEMF (7D).

h

$$BE \cong (a_v * A_s) - (a_s * A_s^{2/3}) - (a_c * \frac{Z^*(Z-1)}{A_s^{1/3}}) - (a_a * \frac{(A_s - 2Z)^2}{A_s}) \pm (\frac{a_p}{\sqrt{A_s}})$$

$$(7C)$$
where $\begin{cases} A_s \cong Z(2+kZ) \\ a_v \cong 15.78 \text{ MeV}; a_s \cong 18.34 \text{ MeV}; a_c \cong 0.71 \text{ MeV}; \end{cases}$

$$a_a \cong 23.21 \text{ MeV}; a_p \cong 12.0 \text{ MeV};$$

Binding energy per nucleon can be estimated with,

$$\frac{BE}{A_{s}} \cong \frac{1}{A_{s}} \begin{bmatrix} (a_{v} * A_{s}) - (a_{s} * A_{s}^{2/3}) - (a_{c} * \frac{Z * (Z - 1)}{A_{s}^{1/3}}) \\ - (a_{a} * \frac{(A_{s} - 2Z)^{2}}{A_{s}}) \pm \left(\frac{a_{p}}{\sqrt{A_{s}}}\right) \end{bmatrix}$$
(7D)

For light, medium and heavy atomic nuclides, fit are reasonable.

7. REVIEW ON NUCLEAR BINDING ENERGY SCHEME

In this section, we try to infer and review relation (7A) for its best possible physics back ground. With further study, nuclear stability and binding

energy can be understood with Up and Down quarks.

We propose that,

(1) Nuclear unit radius can be expressed as,

$$R_0 \approx \frac{2G_s m_p}{c^2} \approx 1.239291 \text{ fm}$$
(2)
$$B_0 \approx \left(\frac{1}{\alpha_s}\right) \left(\frac{e^2}{4\pi\varepsilon_0 R_0}\right) \approx \frac{e^2_s}{4\pi\varepsilon_0 R_0} \approx \frac{e^2_s}{8\pi\varepsilon_0 (G_s m_s/c^2)} \approx 10.09 \text{ MeV}$$

can be considered as the 'unique' binding energy coefficient. Here, we wish to emphasize the point that, the proposed energy coefficient 10.09 MeV is directly connected with nuclear potential and strong coupling constant whereas energy coefficients of various semi empirical formulae are so chosen to fit the mass data and no way connected with strong interaction. Hence our proposed 10.09 MeV can be called as "unique". With reference to the recommended [24] up quark rest energy of 2.15 MeV and down quark rest energy of 4.7 MeV, it is quite interesting to note that,

$$\frac{\left[(2m_u + m_d)c^2 + (m_u + 2m_d)c^2\right]}{2} \approx 10.275 \text{ MeV}.$$

- (3) For increasing (Z, A), all nucleons will not involve in nuclear binding energy scheme.
- (4) The new numbers (f and k) seem to play an interesting role in understanding nuclear stability and binding energy. Both can be considered as the characteristic outcomes of the combined effect of strong and electromagnetic coupling constants. We noticed that,

For Z < 30 and
$$A_s \cong Z(2+kZ)$$
,
 $(B_{A_s}) \cong \left(\frac{Z}{30}\right)^{0.08} \left\{ A_s - \left[\left(0.00189N_s^2 \right) + \frac{1}{2} \right] \right\} 9.16 \text{ MeV} \right\}$
where,
 $\left\{ \frac{\frac{e_s^2}{8\pi\varepsilon_0 \left(G_s m_p / c^2 \right)} - \left(\frac{e^2}{4\pi\varepsilon_0 R_0} \right) \cong 8.928 \text{ MeV} \right\}$
 $\left\{ \frac{e_s^2}{8\pi\varepsilon_0 \left(G_s m_p / c^2 \right)} - \frac{3}{5} \left(\frac{e^2}{4\pi\varepsilon_0 R_0} \right) \cong 9.395 \text{ MeV} \right\}$
and $\frac{8.928 + 9.395}{2} \cong 9.16 \text{ MeV}$
For $Z \ge 30$ and $A_s \cong Z(2+kZ)$,
 $\left(B_{A_s} \right) \cong \left\{ A_s - \left[\left(0.00189N_s^2 \right) + \frac{1}{2} \right] \right\} 9.16 \text{ MeV} \right\}$

$$(k, f) \cong \left(\frac{\left(1-\alpha_s\right)^n}{2n-1}\right) \alpha \cong (0.00646, 0.001904)$$
 where

 $n \cong 1, 2$; It needs further study.

(5) Nucleons that are not involving in nuclear binding energy scheme can be called as 'free nucleons' and can be represented by $A_f \cong f \times A\sqrt{ZN}$ where the coefficient $f \cong 0.00189$ can be called as 'Free nucleon number coefficient'. With reference to the semi empirical mass formula. quantitatively, $f \cong 2(a/b)$ $)^2$ ~ 0.0018753 where

$$f \cong 2(a_c/a_a) \cong 0.0018/53$$

$$a_c = 0.71 \text{ MeV}$$
 and $a_a = 23.21 \text{ MeV}$.

(6) Nucleons that involve in nuclear binding energy scheme can be called as 'active nucleons' and can be represented by

 $A_a \cong A - A_f \cong A \left(1 - 0.00189 \sqrt{ZN} \right).$

- (7) For Z = 11 to 92, when $(A_a 2Z) \cong 0$, corresponding A seems to represent the possible existence of lower stability line.
- (8) The ad-hoc coefficient 0.00189 somehow, seems to lie between $\{s \ge 0.0016 \text{ and } k \ge 0.0064\}$. With reference to electromagnetic interaction, we consider, $[k/\ln(30)] \approx 0.00189$ where 30 is а characteristic representation of atomic number below which nuclear binding strength is approximately $[Z/30]^{\sqrt{k}}(1/\alpha_s) \cong [Z/30]^{0.08} \times 8.68$. From Z=30 onwards, strength of nuclear binding energy remains constant at $(1/\alpha_s) \cong 8.68$. Based on this concept, for Z = (2 to 118), close to stable mass numbers, binding energy [8] can also be approximated with,

(8)

- (9) Binding energy can be assumed to decrease with increasing radius.
- (10)Decreasing proton-neutron ratio seems to play an interesting role in increasing binding energy.
- (11)Considering isotopes, stable mass number plays an interesting role in estimating the binding energy of other stable and unstable isotopes in the form of

 $\left(\left(A_{s}-A\right)^{2}/A_{s}\right)$. This can be considered as

a representation of asymmetry about the mean line of stability. It needs further investigation.

- (12)In case of Deuteron, there exists no strong interaction between proton and neutron [14,17].
- (13)Above and below the stable mass numbers, binding energy can be *approximated* with,

$$B_{A} \cong \begin{cases} \left(1 - 0.00189\sqrt{ZN}\right)A - A^{1/3} \\ -\left(\frac{Z}{N}\right) - \frac{\left(A_{s} - A\right)^{2}}{A_{s}} \end{cases} B_{0}$$
(10A)

Here in this expression, one can find four simple terms. They can be expressed as,

Term-1:

$$\left(1 - 0.00189\sqrt{ZN}\right)A \times B_0$$

Term-2:

$$-A^{1/3} \times B_0$$

Term-3:

$$-\left(\frac{Z}{N}\right) \times B_0$$

Term-4:

$$-\frac{\left(A_{s}-A\right)^{2}}{A_{s}}\times B_{0}$$

Binding energy estimated with relation (10A) can be compared with the following standard semi empirical mass formula.

$$BE \cong (a_v * A) - \left(a_s * A^{2/3}\right) - \left(a_c * \frac{Z * (Z - 1)}{A^{1/3}}\right) - \left(a_a * \frac{(A - 2Z)^2}{A}\right) \pm \left(\frac{a_p}{\sqrt{A}}\right)$$
(10B)

See Fig. 2 for the estimated isotopic binding energy of Z=50. Dotted blue curve plotted with relations (5) and (10A) can be compared with the green curve plotted with relation (10B). Based on Figs. 1 and 2, it is possible to say that,

- a) Relations (5), (7), (10A) and (10B) can also be given some priority in understanding nuclear binding energy scheme.
- b) Estimated binding energy can also be compared with spherical Relativistic Continuum Hartree-Bogoliubov (RCHB) theory data [22] and Thomas-Fermi model (Table of nuclear masses, nsdssd.lbl.gov, 1994).
- c) For (N < Z) and $(N \approx Z)$ estimated binding energy seems to be increasing compared to SEMF estimation.
- d) For $(A >> A_s)$, estimated binding energy seems to be decreasing compared to SEMF estimation.
- e) Modifying third and fourth terms into a new

term of the form $\left(1 + \frac{\left(A_s - A\right)^2}{A_s}\right)$ binding energy for $\left(A \ll A_s\right)$ and $\left(A \gg A_s\right)$ can be

understood.

8. TO ESTIMATE QUARK MASSES

In our earlier paper [25], we proposed that,

- a) Up, Strange and Bottom quarks are in geometric series.
- b) Down, Charm and Top quarks are in another geometric series.

We modify these ideas as:

- a) Down and Up quarks are ground state particles and their mass ratio is 2.
- b) Strange and Bottom quarks are first generation particles having a geometric series with a geometric ratio of, $g_u \approx \sqrt{m_p/m_e} \approx \sqrt{1836.152} \approx 42.85$.
- c) Charm and Top quarks are second generation particles having another geometric series with a geometric ratio of, $g_d \simeq (1/\alpha) \simeq 137.036$.
- d) These two geometric ratios can be fitted with $\frac{e^2}{4\pi\varepsilon_0 G_s m_p m_e} \cong 4.547665.$



Fig. 1. Binding energy per nucleon close to stable mass numbers of Z = 3 to 118



Fig. 2. Isotopic binding energy of Z=50

Considering Up and Down quarks as ground state particles, quark masses [24] can be fitted in the following way.

Step-1: To fit Up quark mass

$$\frac{e^{2}}{4\pi\varepsilon_{0}G_{s}m_{p}m_{u}} \cong 1 \text{ and}$$

$$\frac{G_{s}m_{p}}{c^{2}} \cong \frac{e^{2}}{4\pi\varepsilon_{0}(m_{u}c^{2})}$$
(11)
$$\rightarrow m_{u}c^{2} \cong 2.324 \text{ MeV}$$

Step-2: To fit Down quark mass

$$\frac{m_a c^2}{m_a c^2} \cong 2 \quad \text{and} \\
m_a c^2 \cong 4.648 \text{ MeV}$$
(12)

$$\frac{e^2}{4\pi\varepsilon_0 G_s m_p m_d} \cong \frac{1}{2}$$
(13)

Based on the estimated up and down quarks, we noticed that,

$$\frac{m_u c^2 + m_d c^2}{m_n c^2} \cong 0.0074256 \cong \alpha$$
(14)

where m_n = average mass of nucleon and α = fine structure constant.

Step-3: To fit Strange and Bottom quark masses

Considering Strange and Bottom quarks as first generation particles, their masses can be fitted with,

$$m_{s}c^{2} \simeq \sqrt{\frac{m_{p}}{m_{e}}} (m_{s}c^{2}) \simeq 99.578 \text{ MeV}$$
 (15)

$$m_{b}c^{2} \cong \left(\sqrt{\frac{m_{p}}{m_{e}}}\right)^{2} \left(m_{u}c^{2}\right)$$

$$\cong \left(\frac{m_{p}}{m_{e}}\right) \left(m_{u}c^{2}\right) \cong 4266.95 \text{ M eV}$$
(16)

Step-4: To fit Charm and Top quark masses

Considering Charm and Top quarks as second generation particles, their masses can be fitted with,

$$m_c c^2 \simeq 2 \left(\frac{1}{\alpha}\right) (m_d c^2) \simeq 1273.806 \text{ MeV}$$
 (17)

$$m_{_{I}}c^{^{2}} \cong 2\left(\frac{1}{\alpha}\right)^{^{2}}\left(m_{_{d}}c^{^{2}}\right) \cong 174557.2 \text{ MeV}$$
 (18)

Step-5: To fit the two geometric ratios

Let,

$$\frac{e^2}{4\pi\varepsilon_0 G_s m_p m_e} \cong 4.547665 \cong X$$
(19)

Based on this definition, we noticed that,

$$(g_u, g_d) \cong (e^x - X) \mp \left(\frac{e^x}{2}\right)$$
 (20)

$$g_{u} \cong \left(e^{x} - X\right) - \left(\frac{e^{x}}{2}\right) \cong 42.6582$$

$$g_{d} \cong \left(e^{x} - X\right) + \left(\frac{e^{x}}{2}\right) \cong 137.069852$$
(21)

9. RESULT ORIENTED DISCUSSION

(1) With our long experience in this field, we consider the following four relations as REFERENCE relations [10,17,18]. They need further investigation.

$$A) \quad \frac{m_p}{m_e} \approx 2\pi \sqrt{\frac{4\pi\varepsilon_0 G_e m_e^2}{e^2}}$$

$$B) \quad \hbar c \approx \frac{\left(G_e^2 G_N\right)^{1/3} m_p^4}{m_e^2}$$

$$C) \quad \frac{m_p}{m_e} \approx \left(\frac{G_s}{G_e^{1/3} G_N^{2/3}}\right)^{1/7}$$

$$D) \quad \frac{G_w}{G_N} \approx \left(\frac{m_p}{m_e}\right)^{10}$$

$$(22)$$

Note points:

- a) Relation (22A) is our given definition for G_e .
- b) Inserting (22B) in relation (23), relation (22C) can be obtained.

- c) Relation (22D) can be inferred from relation (32).
- d) With further study, other possible relations for G_e and other set of REFERENCE relations can also be developed.
 - (2) The fundamental question to be answered is: How to justify the estimated values of (G_N, G_s, G_w) with respect to defined G_e ? With reference to current literature pertaining to gravity, it seems impossible to answer this question. By considering 'quantum gravity', it seems possible to find an answer. We noticed that,

$$\left(\frac{G_s m_p}{c^2} / \sqrt{\frac{G_N \hbar}{c^3}}\right) \cong \left(\frac{m_p}{m_e}\right)^6 \left\{ \frac{G_s m_p}{c^2} / \sqrt{\frac{G_N \hbar}{c^3}}\right)^{\frac{1}{6}} \cong \left(\frac{m_p}{m_e}\right) \right\}$$
(23)

In a simplified form,

$$\frac{G_s^2 m_p^2}{G_N \hbar c} \cong \left(\frac{m_p}{m_e}\right)^{12}$$
(24)

a) Considering CODATA-2014 (Committee on Data for Science and Technology) recommended big $G \equiv G_N$, with relation (24) value of G_s can be estimated.

$$G_s \cong \left(\frac{m_p^5}{m_e^6}\right) \sqrt{G_N \hbar c}$$
(25)

b) By inserting the values of (G_N, G_s) in relation (22C), value of G_e can be estimated.

$$G_e \cong \left(\frac{m_e}{m_p}\right)^{21} \frac{G_s^3}{G_N^2} \tag{26}$$

c) By inserting the value of G_e in relation (22A), value of (m_p/m_e) can be estimated.

$$A) \left(\frac{m_p}{m_e}\right) \approx 2\pi \sqrt{\frac{4\pi\varepsilon_0 G_e m_e^2}{e^2}} \text{ (Or)}$$

$$B) \left(\frac{m_p}{m_e}\right) \approx \sqrt{\frac{2\pi\sqrt{\frac{4\pi\varepsilon_0 \hbar^{3/2} c^{3/2}}{e^2 G_N^{1/2} m_e}}}\right)$$
(27)

Calculating the % error in the estimated (m_p/m_e) , error in G_N can be reviewed. % error means–

 $\begin{pmatrix} \frac{\text{Recom.value of } (m_p/m_e) - \text{Estim.value of } (m_p/m_e)}{\text{Recom.value of } (m_p/m_e)} \end{pmatrix} \times 100$ Based on relation (27A) estimated $(m_p/m_e) \cong 1836.549774$ is 216 ppm higher than

the recommended $\left(m_p / m_e\right)$.

A note about 'ppm': It is a commonly accepted relative notation of representation of any measured quantity expressed as number of Parts Per Million.

d) Based on relation (27B), estimated $(m_p/m_e) \cong 1836.251941$ is 54 ppm higher than the recommended (m_p/m_e) . It is surprising to note that, independent of all the proposed three atomic gravitational constants,

$$G_{N} \approx \left(\frac{m_{e}}{m_{p}}\right)^{14} \left(\frac{4\pi\varepsilon_{0}\hbar c}{e^{2}}\right)^{2} \left(\frac{16\pi^{4}\hbar c}{m_{p}^{2}}\right)$$
$$\approx \left(\frac{m_{e}}{m_{p}}\right)^{14} \left(\frac{1}{\alpha}\right)^{2} \left(\frac{16\pi^{4}\hbar c}{m_{p}^{2}}\right)$$
(28)

 $\approx 6.679855429 \times 10^{-11} \text{ m}^3 \text{kg}^{-1} \text{sec}^{-2}$ where, $\alpha \approx$ Fine structure constant

$$A) \left(\frac{m_p}{m_e}\right) \approx \left\{\frac{4\pi^2}{\alpha} \sqrt{\frac{\hbar c}{G_N m_p^2}}\right\}^{1/7}$$

$$B) \alpha \approx 4\pi^2 \left(\frac{m_e}{m_p}\right)^7 \sqrt{\frac{\hbar c}{G_N m_p^2}}$$
(29)

Based on relation (29), by estimating the error in (m)

 $\left(\frac{m_p}{m_e}\right)$ or α , G_N value can be reviewed.

- e) By considering (m_p/m_e) and (α) as key tools, actual G_N value seems to be higher than the CODATA and other big G experimental values. With further study and considering other possible relations for G_e and repeating the above steps, G_N can be refined.
- f) Applying the concept of Penrose model of extraction of black hole energy [26] to a proton, it is also possible to show that [27],

$$\left(1 - \frac{1}{\sqrt{2}}\right) \frac{m_p}{m_e} \cong \left(\frac{\hbar c}{G_N m_p^2}\right)^{1/14}$$
(30)

where,
$$\left\{\frac{4\pi^2}{\alpha}\right\}^{\frac{1}{7}} \cong 3.414393 \cong 2 + \sqrt{2} \cong \left(1 - \frac{1}{\sqrt{2}}\right)^{-1}$$

$$G_N \cong \left[\left(1 - \frac{1}{\sqrt{2}}\right)\frac{m_p}{m_e}\right]^{-14} \left(\frac{\hbar c}{m_p^2}\right)$$
(31)

 $\approx 6.674946866 \times 10^{-11} \text{ m}^3 \text{kg}^{-1} \text{sec}^{-2}$

This estimated value is 130 ppm higher than the, CODATA-2014, recommended value. At the same time, it seems to lie in between experiment carried out by HUST-AAF-2018 result of $6.674484 \times 10^{-11} \text{ m}^3 \text{kg}^{-1} \text{sec}^{-2}$ and BIPM-2014 result of $6.67554 \times 10^{-11} \text{ m}^3 \text{kg}^{-1} \text{sec}^{-2}$. See Table 1 for the historical results [28-35] of G_N .

About HUST-AAF-2018: It is an experiment designed to measure big G with Angular-Acceleration Feedback (AAF) method performed at Huazhong university of science & technology, Hongshan District, Wuhan, Hubei province, China.

About BIPM: The International Bureau of Weights and Measures (IBWM) (French: Bureau international des poids et mesures (BIPM)) is an intergovernmental organization that was established by the Metre Convention, through which member states act together on matters related to measurement science and measurement standards (i.e. the International System of Units). The organization is commonly referred to by its French initialism, BIPM. The BIPM's secretariat and formal meetings are housed in the organizations headquarters in Sevres, France.

(3) Fermi's weak coupling constant is one of the most critical and complicated nuclear physical constants. It can be approximated as,

$$G_{F} \approx \left(\frac{m_{e}}{m_{p}}\right)^{2} \hbar c R_{0}^{2}$$

$$\approx \left[\left(G_{e}^{2} G_{N}\right)^{1/3} m_{p}^{2}\right] \left(\frac{2G_{s} m_{p}}{c^{2}}\right)^{2}$$

$$\approx \left(\frac{m_{p}}{m_{e}}\right)^{10} \frac{4G_{N} \hbar^{2}}{c^{2}} \approx \frac{4G_{w} \hbar^{2}}{c^{2}}$$

$$\approx 1.44021048 \times 10^{-62} \text{ J.m}^{3}$$
(32)

This estimated value is 3036 ppm higher than the recommended value,

$$G_F \cong 1.435850984 \times 10^{-62} \text{ J.m}^3$$
 where
 $G_F / (\hbar c)^3 \cong 1.1663787 \times 10^{-5} \text{ GeV}^{-2}$ [31].

(4) The basic question to be answered is: How do the invoked four gravitational constants address the issues pertaining to vector forces of electromagnetism, tensor forces of gravity and vector-axial vector forces of weak interaction and gluons of strong interaction? It needs further study with respect to the four gravitational constants and the compound (ħ). In this context, we could notice that, 'Range of four interactions' can be expressed by a model relation of the form [27],

$$r_x \approx \frac{M_x}{m_p} \sqrt{\frac{G_x \hbar}{c^3}}$$
(33)

where M_x, G_{x,m_p} represent the characteristic mass of interaction, characteristic gravitational constant and proton mass respectively. As most of the atomic matter is characterised by protons, this relation can be given some consideration.

a) Strong interaction range,

$$r_s \approx \sqrt{G_s \hbar/c^3} \approx 0.361 \times 10^{-15} \text{ m}$$
 (34)

b) Weak interaction range,

$$r_w \approx (80400 \text{ MeV}/938.272 \text{ MeV}) \sqrt{G_w \hbar/c^3}$$
 (35)
 $\approx 2.892 \times 10^{-17} \text{ m}$

c) Electromagnetic interaction range at atomic level,

$$r_{em} \approx (931.5 \text{ MeV}/938.272 \text{ MeV}) \sqrt{G_e \hbar/c^3}$$
 (36)
 $\approx 9.57 \times 10^{-12} \text{ m} \approx 9.57 \text{ pm}$

d) Gravitational interaction range for Sun,

$$r_{sun} \approx (2.0 \times 10^{30} \text{kg}/1.672 \times 10^{-27} \text{kg}) \sqrt{G_N \hbar/c^3}$$
 (37)
 $\approx 1.933 \times 10^{22} \text{ m}$

10. SPECIFIC UNIFIED RELATIONS CONNECTED WITH NUCLEAR RADIUS AND BOHR RADIUS

Characteristic Schwarzschild radius of proton and Schwarzschild radius of atom can be addressed with the following relations.

$$R_{p} \cong \frac{2G_{s}m_{p}}{c^{2}} \cong 1.2393 \text{ fm}$$
(38)

= Characteristic nuclear charge radius [36,37]

$$R_{(Z,A)} \cong \left\{ Z^{1/3} + \left(\sqrt{Z(A-Z)} \right)^{1/3} \right\} \left(\frac{G_s m_p}{c^2} \right)$$
(39)
= Nuclear charge radius [38]

- Ruelear enarge radius [50]

$$a_{0} \cong \left(\frac{4\pi\varepsilon_{0}G_{e}m_{e}^{2}}{e^{2}}\right) \left(\frac{G_{s}m_{p}}{c^{2}}\right) \cong 5.2918 \times 10^{-11} \text{ m}$$
(40)
= Bohr radius of Hydrogen atom [39,40]

| Experiment/Year | $G_N / 10^{-11} \text{ m}^3 \text{kg}^{-1} \text{sec}^{-2}$ |
|-----------------|---|
| NIST-1982 | 6.67248 |
| TR&D-1996 | 6.6729 |
| LANL-1997 | 6.67398 |
| UWash-2000 | 6.674255 |
| BIPM-2001 | 6.67559 |
| UWup-2002 | 6.67422 |
| MSL-2003 | 6.67387 |
| HUST-2005 | 6.67222 |
| UZur-2006 | 6.67425 |
| HUST-2009 | 6.67349 |
| JILA-2010 | 6.6726 |
| BIPM-2014 | 6.67554 |
| LENS-2014 | 6.67191 |
| UCI-2014 | 6.67435 |
| HUST-TOS-2018 | 6.674184 |
| HUST-AAF-2018 | 6.674484 |

Table 1. Various experimental values of G_N

11. SPECIFIC UNIFIED RELATIONS CONNECTED WITH PROTON-ELECTRON MASS RATIO

With reference to electroweak interaction,

$$R_{w} \cong \frac{2G_{w}M_{w}}{c^{2}} \cong 6.7494 \times 10^{-19} \text{ m}$$
(41)

= Schwarzschild radius of M_{w}

$$\frac{R_{p}}{R_{w}} \cong \left(\frac{2G_{s}m_{p}}{c^{2}}\right) \div \left(\frac{2G_{w}M_{w}}{c^{2}}\right) \cong \frac{G_{s}m_{p}}{G_{w}M_{w}} \cong \left(\frac{m_{p}}{m_{e}}\right)$$
(42)

With reference to $R_{w} \cong 6.7494 \times 10^{-19} \text{ m}$ and cconsidering $\left(\frac{m_{p}}{m_{e}}\right)$ as a geometric ratio, nuclear radius and atomic radius can be estimated in the

following way.

$$R_{\rm I} \cong \left(\frac{m_{\rm p}}{m_{\rm e}}\right) \left(\frac{2G_{\rm w}M_{\rm w}}{c^2}\right) \cong 1.2393 \text{ fm}$$
(43)

$$R_{2} \cong \left(\frac{m_{p}}{m_{e}}\right)^{2} \left(\frac{2G_{w}M_{w}}{c^{2}}\right) \cong 2.275 \text{ pm}$$
(44)

With reference to electromagnetic gravitational constant, Schwarzschild radius of electron can be addressed with,

$$R_{e} \cong \left(\frac{2G_{e}m_{e}}{c^{2}}\right) \cong 0.48 \text{ nm}$$
(45)

Based on relations (44) and (45) and identifying R_2 and R_2 as characteristic length scales associated with characteristic atomic radius, we noticed that,

$$\sqrt{R_2 R_e} \cong \left(\frac{2\sqrt{G_e G_s} m_p}{c^2}\right) \cong 33.1 \text{ pm}$$
 (46)

 $\cong R_{atom} \cong$ Scwarzschild radius of atom [41]

12. APPLICATIONS of G_e IN ELEMENTARY PARTICLE PHYSICS AND ASTRO-PHYSICS

A) Understanding the recently observed 3.5 keV galactic photon

Recent galactic X-ray studies [42,43] strongly confirmed the existence of a new photon of energy 3.5 keV. So far, its origin is unknown and

unclear. In this context, we propose [15] the following alternative mechanism for understanding the origin of 3.5 keV photon.

1) There exists a characteristic charged small lepton of rest mass,

$$(m_{xl})^{\pm} \cong \sqrt{\frac{e^2}{4\pi\varepsilon_0 G_e}} \cong 1.75 \text{ keV/}c^2$$
(47)

- 2) With pair annihilation mechanism, (m_{xl}) generates a photon of rest energy 3.5keV
- 3) With current and future particle accelerators, $(m_{xl})^{\pm} \cong 1.75 \text{ keV}/c^2$ can be generated.

B) Fitting Muon and Tau rest masses

Experimentally observed [24] Muon and Tau rest masses can be fitted in the following way.

$$m_{(\mu,\tau)}c^2 \cong \left[\gamma^3 + (n^2\gamma)^n \left(\frac{G_e}{G_N}\right)^{1/4}\right]^{\frac{1}{3}} 1.75 \text{ keV}\right\}$$
 (48)

where,

$$\gamma \cong \sqrt{\frac{4\pi\varepsilon_0 G_e m_e^2}{e^2}} \cong 292.187 \text{ and } n = 1 \text{ and } 2$$

For n=1, obtained $m_{\mu}c^2 \cong 106.5$ MeV

n=2, obtained $m_r c^2 \cong 1781.5$ MeV.

At n=3, a new heavy charged lepton of rest energy 42.2 GeV can be predicted.

13. SPECIFIC UNIFIED RELATIONS CONNECTED WITH STELLAR MASS LIMITS

With reference to strong nuclear gravitational constant and astro-physics point of view, by considering nucleon as a characteristic building block, stellar mass limits [44,45] can be understood with a relation of the form,

$$\frac{G_{N}M_{x}}{G_{s}m_{a}} \cong \sqrt{\frac{G_{s}}{G_{N}}}$$
(49)

Thus, characteristic stellar mass limit can be estimated with a very simple relation of the form,

$$M_{X} \cong \left(\frac{G_{s}}{G_{N}}\right)^{\frac{3}{2}} (m_{n}) \cong 9.37 \text{ solar masses}$$
 (50)

Another interesting relation is,

$$\frac{G_{N}M_{x}}{G_{s}\sqrt{m_{s}M_{w}}} \cong \sqrt{\frac{G_{s}}{G_{N}}}$$
(51)

$$M_{x} \cong \left(\frac{G_{s}}{G_{N}}\right)^{\frac{3}{2}} \sqrt{m_{s}M_{w}} \cong 234 \text{ solar masses}$$
 (52)

With reference to electromagnetic gravitational constant, mass limits of super massive stellar objects can be understood.

14. TO UNDERSTAND THE INTEGRAL NATURE OF ELECTRON'S ANGULAR MOMENTUM

Without considering the rest mass of proton, Bohr's theory of Hydrogen atom [40] attempts to explain the discrete spectral lines. On a whole,

- a) If hydrogen atom is characterized by its central mass and central charge,
- b) If mass of proton is 1836 times heavier than electron,

then, ignoring proton mass in the calculation of emitted spectral lines seems to be a fundamental snag. Probably it may be the root cause of failure of developing a unified model. With our approach, it is possible to show that,

$$\hbar c \cong G_{s}M_{w}m_{e} \cong \left(\frac{G_{w}G_{e}}{G_{s}}\right)m_{p}m_{e}$$
(53)

$$\hbar \cong \left(\frac{1}{c}\right) \left(\frac{G_{w}G_{e}}{G_{s}}\right) m_{p}m_{e}$$
(54)

As per the Bohr's second postulate,

$$(m_e vr) \cong n\hbar \cong n \left(\frac{1}{c}\right) \left(\frac{G_w G_e}{G_s}\right) m_p m_e$$
 (55)

where, n = 1, 2, 3, ...

It can be inferred as,

$$m_{e}(vr) \cong \left[\left(\frac{1}{c}\right) \left(\frac{G_{w}G_{e}}{G_{s}}\right) (nm_{p}) \right] m_{e}$$
(56)

Possible interpretation seems to be,

Clearly speaking, integral nature of m_p i.e. m_p , $2m_p$, $3m_p$,... nm_p , seems to be responsible for the integral nature of electron's angular momentum. This explanation seems to be very natural and very simple. We are working in this direction and planning to seek experts' opinion.

15. TO CONFIRM THE EXISTENCE OF $(G_e, G_w G_s)$

- 1) At atomic scale, based on relation (46), there is a possibility of confirming the existence of (G_e, G_s) .
- 2) Neutron life time point of view, there is a possibility of confirming the existence of $(G_{e,}G_{w})$. Interesting point to be noted is that by considering moving neutrons and their relativistic mass expression, results of bottle and beam methods can be correlated [46,47,48]. Its characteristic relation is,

$$t_n \cong \left(\frac{G_e^2 m_n^2}{G_w \left(m_n - m_p\right) c^3}\right) \cong 874.94 \text{ sec} \right\}$$
(58)

- 3) Astrophysics point of view, based on relation (49), there is a possibility of confirming the existence of (G_s) .
- 4) Galactic observations of point of view, based on relation (47), there is a possibility of confirming the existence of (G_e) . We emphasize the point that, compared to the concept of decay of cosmic neutrinos, annihilation of $(m_{xl})^{\pm}$ can be given a priority in understanding the origin of 3.5 keV photons. With particle accelerators, existence of $(m_{xl})^{\pm}$, can be confirmed and thereby existence of (G_e) can also be confirmed.

5) With reference to $T \approx \hbar c^3 / 8\pi k_B (G_s m_p)$ or $T = \hbar c^3 / 8 = \hbar (G_s m_p)$

$$T \approx \hbar c^3 / 8\pi k_B (G_e m_e)$$
 or

 $T \approx \hbar c^3 / 8\pi k_B (G_w m_w)$ and with particle accelerator experiments and by considering the melting points of nucleons, electrons and other characteristic elementary particles, existence of (G_e, G_w, G_s) can be understood.

- 6) With reference to magnetic dipole moments of elementary particles and stellar objects, there is a possibility of confirming the existence of $(G_w G_s)$
- Proton magnetic moment can be estimated with a relation of the form,

$$\mu_{p} \cong \frac{e_{s}\hbar}{2m_{p}} \cong \frac{eG_{s}m_{p}}{2c}$$

$$\cong 1.488 \times 10^{-26} \text{ A.m}^{2}$$
(59)

b) Electron magnetic moment can be estimated with a relation of the form,

$$\mu_{e} \cong \frac{e\hbar}{2m_{e}} \cong \frac{eG_{s}M_{w}}{2c}$$

$$\cong 9.274 \times 10^{-24} \text{ A.m}^{2}$$
(60)

Since, $G_s m_e \cong G_w M_w$, modifying relation (60) leads to,

$$\mu_{e} \cong \left(\frac{M_{w}}{m_{e}}\right)^{2} \frac{eG_{w}m_{e}}{2c}$$

$$\cong 9.274 \times 10^{-24} \text{ A.m}^{2}$$
(61)

c) If mass of stellar object is M_x , with reference to relation (61), stellar magnetic dipole moments [49,50], can be expressed as,

$$\mu_{x} \cong \left[1 + \left(\frac{M_{w}}{M_{x}}\right)^{2}\right] \left(\frac{eG_{w}M_{x}}{2c}\right) \cong \left(\frac{eG_{w}M_{x}}{2c}\right) \\ \text{since}, \left(\frac{M_{w}}{M_{x}}\right) << 1 \text{ and } \left[1 + \left(\frac{M_{w}}{M_{x}}\right)^{2}\right] \cong 1$$
(62)

Since any stellar object mass is mainly influenced by nucleon mass, based on relations (59) and (62) and based on the

known and unknown internal structural or binding forces, lower, upper and mean values of stellar magnetic moments can be expressed as,

$$(\mu_{x})_{lower} \cong \left(\frac{eG_{w}M_{x}}{2c}\right)$$

$$(\mu_{x})_{upper} \cong \left(\frac{eG_{s}M_{x}}{2c}\right)$$

$$(\mu_{x})_{mean} \cong \left(\frac{e\sqrt{G_{w}G_{s}}M_{x}}{2c}\right)$$

$$(63)$$

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With reference to strong and weak interactions, it is possible to say that,

i. If stellar object is strongly bound, then it can have a maximum magnetic moment and can

be expressed by
$$\left(\frac{eG_sM_x}{2c}\right)$$

- ii. If stellar object is weakly bound, then it can have a minimum magnetic moment and can be expressed by $\left(\frac{eG_{w}M_{x}}{2c}\right)$.
- iii. To a very rough approximation, mean magnetic dipole moment can be approximated with a relation of the form, $\left(e \sqrt{G_w G_s} M_x \right)$

$$\left(\frac{c_{V}G_{w}G_{s}M_{x}}{2c}\right)$$

- iv. Earth's estimated mean magnetic dipole moment is $4.986 \times 10^{22} A.m^2$ and actual value $8 \times 10^{22} A.m^2$.
- v. Sun's, estimated mean magnetic dipole moment is $1.65 \times 10^{28} A.m^2$ and actual value $3.5 \times 10^{29} A.m^2$.
- vi. With reference to other stellar compact objects and black holes, further study can be carried out.

16. GENERAL DISCUSSION

We appeal that,

- Success of any unified model depends on its ability to involve gravity in microscopic models.
- (2) Full-fledged implementation of gravity in microscopic physics must be able to:
 - a) Estimate the ground state elementary particle rest masses of the three atomic interactions.

- b) Estimate the coupling constants of the three atomic interactions.
- c) Estimate the range of all interactions.
- d) Estimate the Newtonian gravitational constant.
- (3) As the root is unclear and unknown, to make it success or to have a full-fledged implementation, one may be forced to consider a new path that may be out-ofscope of the currently believed unsuccessful unified physics.
- (4) In our approach,
 - a) We assign a different gravitational constant for each basic interaction.
 - b) We consider proton and electron as the two characteristic building blocks of the four basic interactions.
 - c) Finally, by eliminating the three atomic gravitational constants, we develop a characteristic relation for estimating the Newtonian gravitational constant. Based on relations (1) and (29), it is possible to show that,

$$\frac{m_{p}}{m_{e}} \cong \frac{G_{w}^{13/4} G_{e}^{3/2}}{G_{s}^{9/2} G_{N}^{1/4}}$$
(64)

$$G_{N} \cong \left(\frac{m_{e}}{m_{p}}\right)^{4} \frac{G_{w}^{13}G_{e}^{6}}{G_{s}^{18}} \cong \frac{G_{w}^{21}G_{e}^{10}}{G_{s}^{30}}$$
(65)

- d) During this journey, without considering arbitrary numbers or coefficients, we come across many strange and interesting relations for estimating other atomic and nuclear coupling constants.
- (5) We strongly believe that, with further study, research and synthesizing the noticed relations in a systematic approach, actual essence of final unification can be understood in a theoretical and experimental approach [51]. In addition to that, magnitudes of elementary physical constants can be reviewed in a unified approach.
- (6) During cosmic evolution [52], if one is willing to give equal importance to Higgs boson and Planck mass in understanding the massive origin of elementary particles, then it seems quite logical to expect a common relation in between Planck scale and Electroweak scale [53,54,55].

17. CONCLUSION

By implementing four such gravitational constants in String theory models, it may be

possible to explore the hidden unified physics connected with compound $(\hbar c)$, different forms of fundamental forces and their interaction ranges. Even though derivational procedure is missing, consequences of the proposed four reference relations (22A, 22B, 22C and 22D) seem to be quite interesting and logical. Based on relations (1A,1B,1C and 1D) and with further study, research and confirming the existence of $M_{\odot}c^2 \cong 584.725 \text{ GeV}$, actual essence of final unification can be understood. Independent of large numbers, gap between nuclear scale and Planck scale can be understood via relations like (23) and (33) with proper physics. Considering the applications proposed in sections (10 to 15), to some extent, existence of (G_{a}, G_{a}, G_{u}) can be validated. Finally, theoretical value of G_{y} can be defined as a standard reference for future nuclear, atomic and gravitational experiments.

Understanding nuclear binding energy with single energy coefficient in terms of fundamental interactions is a very challenging task. In this context, we tried our level best in presenting a very simple and effective semi empirical formula with one unique energy coefficient. It needs further investigation.

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COMPETING INTERESTS

Authors have declared that no competing interests exist.

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